UDC 539.17: 539.142/.144 AN ANALYSIS OF CROSS-SECTIONS OF 9BE+28SI INTERACTION IN THE FRAMEWORK OF THE DOUBLE-FOLDING MODEL

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In this paper the experimental data on the differential cross sections for elastic scattering of ⁹Be ions on ²⁸Si nucleus at the energies of the incident nucleus ranging from 12 to 201.6 MeV were analyzed in the framework of the double-folding model using the Paris NN-potential CDM3Y. A good agreement with the experimental angular distributions of differential cross sections for elastic scattering was obtained and the values of the total reaction cross sections were calculated. When the double-folding potential was used as real and imaginary parts, no manifestation of the threshold anomaly was detected. The reason for such a behavior of the potential can be explained by the presence of break-up and/or transfer channels at low energies.

Introduction.

It was found that a decrease in the energy of incident particles, i.e. a decrease in the number of open channels, must cause a reduction in the imaginary part of the potential and its vanishing at energies close to the Coulomb barrier. This phenomenon is called a threshold anomaly [1, 2].

However, for weakly-bound nuclei the situation is quite different. In systems where a weaklybound nucleus interacts with a nucleus of the target, there is a strong connection between the elastic scattering channel and other channels (break-up or transfer of nucleons) [3]. In this case, due to the presence of these additional channels, the reaction has a large cross section and, hence, the imaginary part of the potential cannot decrease and tend to zero with decreasing energy. An analysis of the experimental results aimed at studying of elastic and inelastic scattering of nuclei - the processes most sensitive to the geometric dimensions of the nuclei (the density distribution of nucleons in the nucleus) and their potential interactions - as a rule, uses both macroscopic and microscopic approaches. To obtain information about the nucleus structure it is necessary to gain a detailed knowledge of the mechanism of nucleus-nucleus interaction, which includes construction of nucleus-nucleus optical potentials.

The problem of ambiguity of potential parameters is a typical problem for macroscopic optical potentials obtained from the analysis of differential cross sections for elastic scattering. The microscopic models will enable us to avoid the use of phenomenological parameters and advance in the description of the properties of atomic nuclei.

Firstly, the model takes into account the structural description of the nucleus (the matter density distribution), secondly, the nucleon-nucleon potential takes into account interaction at the microscopic level and depends on the density of nucleons within the nucleus. In such models the real part of the potential is usually calculated on the basis of the double-folding model, whereas the imaginary part remains phenomenological and is chosen in the Woods-Saxon form.

⁹Be nucleus is a loosely bound cluster with a small binding energy of a neutron (1.665 MeV) and an alpha-particle (2.55 MeV). ⁹Be has no bound excited states at energies lower than 1.665 MeV. Therefore, interaction of ⁹Be with ²⁸Si must have specific features mentioned above.

Investigations of ⁹Be scattering gave contradictory results. In the experiments on scattering of ⁹Be on ²⁷Al nuclei at 12-47 MeV [9], on ⁶⁴Zn nuclei at 17-28 MeV [10, 11] and on ²⁰⁹Bi nuclei at 35-50 MeV [12, 13] no threshold anomaly was discovered, whereas scattering of ⁹Be nucleus on ²⁰⁸Pb nucleus [14] showed such an anomaly.

In this paper we present the results of a joint analysis of angular distributions of differential and total reaction cross sections (σ_r) for the ⁹Be+²⁸Si interaction in the framework of the double-folding model, in which the imaginary part of the potential is obtained on the microscopic basis.

Analysis of the Experimental Data. Differential cross sections for elastic scattering of ⁹Be on ²⁸Si nucleus were obtained using the potential calculated by the DFM-POT program [5], on the basis of the double-folding model.

The potential of interaction of two colliding nuclei in the first order in effective forces can be written as:

$$V^{DF} = V^D + V^{EX} \tag{1}$$

where V^D is the potential of direct folding,

V^{EX} is the potential taking into account the nucleon exchange.

There are several types of potentials of effective nucleon-nucleon forces v_{NN} . We used the Paris potential CDM3Y [6], which has the following form:

$$\mathbf{v}_{NN}(\mathbf{E}, \boldsymbol{\rho}, \mathbf{s}) = \mathbf{g}(\mathbf{E})\mathbf{F}(\boldsymbol{\rho})\mathbf{v}(\mathbf{s}), \tag{2}$$

The total optical potential usually consists of the real and imaginary parts. In our case, it was assumed that the imaginary part of the potential has the same radial shape as the real part and we use the same double-folding potential, but with a different normalization factor.

$$U(r) = N_r V^{DF}(r) + i N_w V^{DF}(r) + V_C(r),$$
⁽³⁾

where N_{r,w} are factors normalizing the depth of the real and imaginary parts, respectively, which varied in order to get the best fit with the experimental data on the differential cross sections and the total reaction cross sections. The last term $V_C(r)$ in (3) is the Coulomb potential, which is assumed to have the form of a uniformly charged sphere of a radius $R_C = 1.25(A_p^{1/3} + A_t^{1/3})$, where Ap and At are mass numbers of the projectile nucleus and the target nucleus, respectively.

The code FRESCO has been used for the calculations [8]. Parameters N_r and N_w , giving the best correspondence between the experimental and theoretical values of cross sections were found by the minimization of the quantity:

$$\chi^{2} = \frac{1}{N_{\text{exp}}} \sum_{i=1}^{N_{\text{exp}}} \left[\frac{\sigma^{\text{theor}}(\theta_{i}) - \sigma^{\text{exp}}(\theta_{i})}{\Delta \sigma^{\text{exp}}(\theta_{i})} \right]^{2}, \qquad (4)$$

where N_{exp} is the number of experimental points in the angular distribution,

 σ^{theor} and σ^{exp} are calculated and measured values of the differential scattering cross section at an angle θ_i ,

and $\Delta \sigma^{exp}$ is the uncertainty of $\sigma^{exp}(\theta_i)$.

The optimal parameters of the double-folding potential for elastic scattering of ⁹Be on ²⁸Si nucleus, the values of \Box ²/*N* and the values of the volume integrals of real J_v and imaginary J_w parts of potentials are presented in Table 1.

Table 1 shows that the values of normalizing factors N_r and N_w are in the range 0.350-0.600 [1, 4, 7, 20, 21, 22], it was shown that in order to get optimal description of the experimental data, in the double-folding potential for the interaction of weakly-bound nuclei it is necessary to reduce the depth of the potential by about 60 %. It should be noted that for ⁹Be scattering the ratio of parameters is $N_r/N_w \approx 1.5$, which is similar to the case of ^{6,7}Li scattering.

Table 1- Optical potential parameters.

Энергия (МэВ)	Nr	N _w	<i>Jv/A_pA_t</i> (МэВфм ³)	<i>Jw/A_pA_t</i> (МэВфм ³)	$\left\langle r^{2}\right\rangle _{r}^{1/2}$ (фм)	$\left\langle r^{2}\right\rangle _{w}^{1/2}$ (фм)	□ _{<i>R</i>} (мб)	\Box^2/N
12	0.400	0.605	186.222	281.660	4.651	4.651	276.8	0.204
13	0.400	0.605	186.060	281.415	4.651	4.651	430.4	0.183
14	0.400	0.605	185.898	281.170	4.651	4.651	576.1	0.630
17	0.400	0.605	185.413	280.437	4.651	4.651	921.7	0.328
20	0.400	0.402	184.929	185.853	4.651	4.651	1092	2.799
23	0.485	0.544	223.641	250.847	4.651	4.651	1327	2.271

26	0.485	0.544	223.058	250.193	4.651	4.651	1449	1.140
30	0.485	0.544	222.282	249.322	4.651	4.651	1568	5.192
50	0.400	0.494	180.161	222.500	4.652	4.652	1794	3.908
121	0.346	0.377	146.506	159.633	4.655	4.655	1810	12.574
201.6	0.369	0.368	145.671	145.276	4.660	4.660	1755	9.651

Table 1 presents the values of the real and imaginary parts of the volume integrals of the potential. As is known, the volume integrals of different potential families differ considerably because of discrete ambiguity, but have the same order of magnitude for different types of charged particles, and there are potential families with the same value of $J_{v,w}/A_pA_t$ for different types of incident particles scattered by the same nuclei. We used potential families with $J_v/A_pA_t = 145-224$ MeVfm³ and $J_w/A_pA_t = 145-282$ MeVfm³. The table also gives \Box^2/N values, which, as it is seen, are within the permissible limit.

Figure 2 and Figure shows the results of analysis of angular distributions of differential cross sections for elastic scattering of ⁹Be on ²⁸Si nucleus with potential parameters from Table 1. The figures show a good description of the experimental data in the entire angular range.

The Coulomb barrier for the ${}^{9}\text{Be} + {}^{28}\text{Si}$ interaction is 14.45MeV in the laboratory system. Therefore, in the angular distributions for elastic scattering at 12, 13 and 14 MeV, Rutherford scattering prevails up to 60 °, and parameters used to describe the experimental data at these energies are not sensitive to the nuclear potential.

Figure 3 shows the energy dependence of the normalizing factors N_r , N_w . It is seen that the depth of the real part for the energies near the Coulomb barrier and higher (12-201.6 MeV) is practically independent of energy. The behavior of the imaginary part is different from that of the real part: even at energies below the Coulomb barrier and close to it (12-30 MeV) - the depth of the potential increases and then gradually decreases with increasing energy. This behavior of the potential shows that there is no threshold anomaly for the ⁹Be+²⁸Si reaction in this energy range.



Figure 2 - The elastic scattering angular distributions for ${}^{9}Be+ {}^{28}Si$ at different energies. Points are the experimental data [23, 19], the solid line is the result of calculations using the double-folding potential with the parameters from Table 1.



Figure 3 - The dependence of N_r and N_w on the energy of the incident nucleus.

This is confirmed by the following conclusions. For the ⁹Be+ ²⁸Si system there are open channels of reactions at energies below and near the Coulomb barrier (12- 30 MeV), which is why the imaginary part of the potential does not approach zero at these energies.

⁹Be is a cluster weakly-bound nucleus (${}^{8}\text{Be} + n - S_n = 1.665 \text{ MeV}$, ${}^{5}\text{He} + {}^{4}\text{He} - S_a = 2.55 \text{ MeV}$) and does not have any bound excited states below 1.665 MeV, and therefore, in reactions with its participation, the reaction cross section at sub-barrier energies must increase. The most probable reaction channels for this system are break-up of the nucleus and transfer of the nucleon.

Angular distributions of differential cross sections for elastic scattering of ⁹Be on ²⁸Si nucleus were used to calculate σ_R . Figure 4 shows the experimental data on σ_R for ⁹Be+²⁸Si interaction at the energies of the incident nucleus ranging from 12 to 201.6 MeV, as well as σ_R values, calculated in this work and the results of calculations made in [23, 16] in the framework of the optical model using the Woods-Saxon potential.

Figure 4 shows that at energies close to the Coulomb barrier (12-20 MeV), σ_R increases with an increase in the amount of energy. This confirms the fact that there are open reaction channels in this energy range. It is seen that the results of our calculations are in good agreement with the experimental and earlier calculated values of σ_R .



Figure 4 - Total reaction cross sections for the ⁹Be+ ²⁸Si interaction.

D denotes the experimental data [15]. The solid line is the result of calculation using the doublefolding potential with parameters from Table 1. The dotted line is the result of calculations by the optical model [23], the dashed line is the result of calculations by the optical model [16]. The arrow shows the Coulomb barrier of the reaction.

Conclusion. The experimental data on the differential cross sections for elastic scattering of ⁹Be ions on ²⁸Si nucleus at energies of the incident nucleus ranging from 12 to 201.6 MeV were analyzed in the framework of the double-folding model with the Paris NN-potential CDM3Y.

A significant difference between the behavior of the real and imaginary parts of the potential was revealed: the depth of the real part remains constant and is almost independent of energy at energies higher than the sub-barrier energies, whereas the depth of the imaginary part increases at energies below and near the Coulomb barrier (12-30 MeV) and then gradually decreases with increasing energy. This behavior of the potential shows the absence of the threshold anomaly, which is caused by the presence of break-up and transfer channels at the energies below and near the Coulomb barrier.

The energy dependence of the total reaction cross section for the ⁹Be+²⁸Si interaction was determined and compared with the available experimental and theoretical data.

It should be noted that in this paper the real and imaginary parts of the optical potential were obtained only on the microscopic base. This approach allowed us to get a good description of the experimental data on the differential and total reaction cross sections for the ${}^{9}\text{Be}+{}^{28}\text{Si}$ interaction. These parameters of the potential, describing the experimental date on elastic scattering and total reaction cross sections, make it possible to state that the calculated values of potential parameters are realistic.

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